OUR FINGERS AS AN AID IN MULTIPLICATION. Perhaps one of the most difficult tasks in pedagogy -a task which exacts the utmost patience on the part of both instructor and pupil-is the teaching of the multiplication table. Month after month teachers expend their time and use their skill in demonstrating and explaining by all possible means exactly what the product of two numbers represents. Often enough these efforts have been vainly expended. After the children have apparently mastered those products in which the numbers 7 and 8 occur, they pass to those in which the number 9 figures, and while mastering these, often completely forget the preceding series. As a general rule, the products from 2 to 6 are quickly mastered and easily retained; but in multiplying together numbers greater than 6, the child proceeds slowly. Beyond 12, even adults find mental multiplication difficult, and resort to pencil and paper.
A Polish mathematician, named Procopovitch, has given his attention to this matter of multiplication
a certain number still remains. The fingers remaining on the one hand, multiplied by those left on the other hand, will give the number of units, which, being added to the tens, gives the desired product. For example : Suppose that 8 is to be multiplied by 9 . The middle finger of the right hand is placed against the ringfinger of the left hand, as shown in Fig. 2. Counting the number of fingers above those which have been placed together, including these, seven fingers, representing 7 tens or 70 in the product sought, are obtained. There still remain on the right hand two fingers, which, multiplied by the one finger remaining on the left hand, give 2 as the number of units. These two units added to the tens already obtained give 72, the product of $8 \times 9$. It is, of course, immaterial on which hand the multiplier or multiplicand is taken.
If it is desired to multiply $7 \times 9$, then the same method is employed, the index-finger of one hand being placed against the ring-finger of the other hand, as placed against the ring-finger of the other hand, as
shown in Fig. 3. Counting the number of fingers


Fig. 1.-Multiplying $9 \times 9$.


Fig. 4.-Multiplying $9 \times 6$.


Fig. 7.-Multiplying $8 \times 6$.


Fig. 10.-Multiplying $6 \times 6$.


Fig. 2.-Multiplying $9 \times 8$.


Fig. 5. - Multiplying $8 \times 8$.


Fig. 8.-Multiplying $7 \times 7$.


Fig. 11.-Multiplying $14 \times 13$.
and the results obtained are in every way as remarka ble as those already described. In the first series, com prising numbers of two ciphers, the thumb represents 11 , the index-finger 12 , the middle finger 13 , the ringfinger 14, and the little finger 15 . When multiplying one number by another, the fingers representing the respective factors are placed together as before. The number of fingers above those joined, inclucing these, will in this case also indicate a certain number of tens. The lower fingers are, however, entirely neglected. In order to obtain the number of units, the fingers which have already given the number of tens are again taken the number on the one hand being multiplied by the number on the other hand. The product thus obtained is increased by 100 and the sum added to the number of tens. Suppose that 13 is to be multiplied by 14. As indicated in Fig. 11, the fingers representing these numbers are joined. Counting the number of fingers above those which have been placed together including the latter, 7 tens or 70 are obtained. Taking


Fig. 3.-Multiplying $9 \times 7$.


Fig. 6. Multiplying $8 \times 7$


Fig. 9.-Multiplying $7 \times 6$.


Fig. 12. - Multiplying $16 \times 17$

RAPID METHOD OF MULTIPLICATION WITH THE FINGERS.
and has invented a system which, for ingenuity and hadicity, leaves little to be desired Pir fingers in mathematical computations which wereat all difficult to them, and hence devised a method of manual multiplication that has been successfully used in many European schools. Procopovitch's system neglects all products involving numbers less than 6, because, as we have already observed, these products are readily learned by most children.
The Polish mathematician first numbers the fingers of each hand. The two thumbs each represent 6, the index-fingers 7 , the middle fingers 8 , the ring-fingers 9 and the little fingers 10 . In order to multiply any two of these numbers, the fingers representing the multiplier and the multiplicand are placed end to end. Be ginning with the fingers which have been thus placed together, the number of fingers is counted, proceed ing toward and including the thumbs. The sum will be the number of tens contained in the desired product. Below the fingers which have been joined,
or 60 will be obtained. Multiplying the three finger remaining on 'the right hand by the one left on the other hand, 3 units are obtained, which, added to th 6 tens, give 63 as the product of $9 \times 7$ or $7 \times 9$.
If it is desired to multiply $6 \times 6$, the two thumbs are placed together as shown in Fig. 10. The two thumbs represent here only two tens in the required product there being no other fingers above those joined. Mul tiplying the four remaining fingers on the one hand by the four on the other, 16 is obtained. This added to wenty gives $20+16=36$, the product of $6 \times 6$. Figs. 1 to 10 inclusive represent the multiplication of various factors in the series.
The Polish mathematician does not stop here, but ex tends his system to numbers greater than 10 . In the old method, the multiplication of factors composed of two ciphers involved difficulties which, as we have already observed, could be overcome only with the assist ance of pencil and paper. In this system of manua multiplication these obstacles are easily surmounted
these same fingers again and multiplying the number on one hand by the number on the other hand, the product 12 , representing the number of units, is obtained. Adding to this the constant 100 and the number of tens, there results $70+12+100=182$, the product of $14 \times 13$
Another method could be employed which, although it would lead to the same result, is not so simple. In this second method, the fingers above those which have been joined, including the latter, represent the number of twenties. In Fig. 11, for example, there are on the right hand three fingers and on the left hand four fingers, giving 7 twenties or 140. The remaining fingers, three in number, represent the number of tens, and in this example are equal to 30 . Finally the four fingers on the left hand, representing the twenties, multiplied by the three on the right hand, also representing the twenties, give 12 for the number of units. Adding, there results $140+30+12=182$.
In multiplying two numbers each of which is greater than 15, a new series is employed extending from 16 to
20. In this series the thumb represents 16 and the little finger 20. The fingers placed together added to those above give the number of twenties. The constant to be added in this case is 200 . If it is desired to multiply 16 by 17 , a product not readily obtained by mental calculation, the fingers representing the factors are joined as indicated in Fig. 12. The thumb of the left hand, representing the multiplier, being placed ayainst the index-finger of the right hand, gives, with the remaining thumb, 3 twenties or 60 . The four fingers remaining on the left hand multiplied by the three lower fingers on the right hand give as the number of units 12. Adding to this product the constant 200 and the number of twenties, there results $60+12+200=272$.
In this manner the series can be extended indefinitely, the only condition to be observed being that the mul tiplier and the multiplicand should be members of the same series of five numbers. The entire system of manual multiplication rests on this condition.

## spirit slate writing and rindred PHENOMENA.-III.

We will now describe a trick which is performed with the aid of two double slates, either tied togethe or riveted at the corners. They are, of course, brought to the medium by the unbeliever. Both the medium and the stranger sit at the table, and the slates are held under it, the medium grasping one corner and the skeptic the other corner, each with one hand, and the disengaged hands are clasped together above the table. After a time the slates are laid upon the table the string is untied and the slates are taken apart, but no writing is found. The medium states it must have been because there was no slate pencil, and when a small piece of pencil is placed between the slates.and they are again tied with a cord by the medium, he again passes them under the table, both persons hold ing the slate as before. Presently writing is heard, and, upon the skeptic bringing the slates from under the table and untying the cord himself, he finds one of the slates covered with writing, though but shortly before they were blank. The explanation is simple; the medium does not pass the slates under the table the first time, but drops them in his lap with the side where the string is tied or knotted downward, and really passes a set of slates of his own for the skeptic to hold, the medium supporting his end by pressing against the table with his knee, which leaves his hand disengaged. He now covers the face of the slate which is uppermost in his lap with writing, doing. so very quietly and without noise. As he brings the slates above the table he leaves his own in his lap and brings up the skeptic's with the writing side down. The slates are untied and taken apart and shown devoid of writing on the inside, which he claims was caused by not having any pencil inside. The medium now places the pencil upon the slate which was originally the upper one, covers this with what was the bottom slate, which is covered with writing inside on the back or bottom of the slate. This action brings this slate on top, with the writing upon its inside. The slates are again tied together, and, in doing so, the slates ar turned, bringing the slate containing the writing upon the inside at the bottom. instead of the top; the string is tied or knotted above the top slate. Of course when again separated, the writing is found upon th inside of the lower slate. When the slates are passed under the table the second time, the spectator himself is allowed to do this, and the medium with one of his finger nails, while holding his end of the slate, pro duces a scratching noise on the slate, closely resem bling the tracing of a pencil. The slates may be held above the table the second time if preferred

In case two slates are brought which are riveted or screwed together, another method must be employed The slates are held under the table in the same man ner as in the previous tests: the medium is provided with a hardwood wedge and a piece of thin steel wire at one end of which is.attached a tiny slate pencil. An old umbrella rib is sometimes used, as it has a small eye at the end through which the pencil is forced. The wooden wedge is pushed between the wooden frames of the slates at each side. The frames and slates will give enough to allow the wire and pencil to be inserted and writing being accomplished with it, after which the w:re is withdrawn and then also the wooden wedge. All this is done without leaving any trace or mark behind it. (See Fig. 7.)
Another inethod of slate writing was performed by a prestidigitateur, but the means employed belong rather to the conjurer than to the spiritualist. 'This called for the placing of a slate on a table, and, while the committee held their hands upon the slate, the sound of writing was heard, and in a few moments a message was written upon it. The table had a double top, with roolu enough to conceal a small boy. There was a neatly made trap beneath the table cloth and the top of the table, the cloth being glued around the opening to keep its place. The trap door opened downward, and the boy concealed in the table opened it and did the necessary writing on the slate and again closed the opening. This idea was impro ved upon by dourg away
with the boy and the double-top table. The writing was then done with the lights turned down low, and the medium introduced his hand under the table
opened the trap and did the writing, and shut the trap before the lights were turned up. The medium and the committee sat around the table with their hands resting on the slate and each person's hand touched that of his neighbor, so that neither could nove without the other being aware of the fact, but he medium's right hand neighbor was a confederate. Another method of producing writing upon the in side of two slates sealed together is as follows: Th table is the same as that previously described. Th slates are two single ones hinged together and sealed around the edges in any manner the committee may see fit. One of the slates is a trick slate; the slate tself working on a pivot or hinge along one of its

existing in the match factories of Great Britain, and an investigation revealed such a deplorable state of affairs as led to memorializing the Home Secretary. How far these or simular conditions may obtain in the United States and Canada is not known, and perhaps would be difficult to determine, since the "hands" ar constantly entering and going or shifting. Further, or dinary commercial ("stick") phosphorus is now very ittle employed, thanks to the demand for the "par or" match, which requires the amorphous variety which is nearly odorless, gives off little fumes, and i but slowly and with some difficulty absorbed by the human economy. If handled with ordinary precau tions, amorphous phosphorus is scarcely at all ob jectionable or dangerous; but, unfortunately, the aver age employe is apathetic as regards self, and not at all uclined to adopt measures that entail extra care labor.
Abroad the demand for cheap matches, regardless of character or composition, is much greater than in the United States, and antiquated and cheap methods gen erally obtain. "Stick" phosphorus continues to be used to a degree not known for many years on this side of the Atlantic. On the Continent of Europe, gener ally, however, the governmental paternalism is such that it is possible to throw certain safeguards around actories and employes such as would not be tolerated in English-speaking countries. In France and Belgium, for instance, as well as Germany, Sweden, and Norway certain stringent rules are formulated, that not only uust be printed in large and legible type, and posted conspicuously everywhere throughout a plant, but ar equired to be read as often as once each week to the employes. Further, dining and lunch rooms are pro vided in connection with every establishment, along with suitable clothing and retiring rooms, lavatories, etc. It is enjoined that no food or drink be brough into the building, except as provided for by the man agement; consequently, eating and drinking in the workshops are prevented. Even the chewing of gum is prohibited. Before partaking of any meal, and prio to leaving the factory at the close of the day, each in dividual is required to doff his or her working clothes, and put on uncontaminated garments; the hand must be thoroughly cleansed by means of soft soap and water; the finger nails duly attended to ; teeth cleansed and mouth and throat washed with a gargle specially provided, all of which is enforced by rigid inspection Each person seeking employment, moreover, is care fully su bjected to examination by the medical office of the company, who rejects all under sixteen years o age, all possessed of bodily infirmities of any kind even to a sore or abrasion or slight defect in dentition or who are "delicate" or anæmic ; all must either hav been vaccinated or have secured immunity through smallpox. With the first evidence of illness, regardles of source or character, the employe is suspended, but allowed to draw two-thirds wages until fully recovered Such procedures, aided by efficient methods of ven tilation, have materially lessened the accidents that commonly accrue to the match industry. Among the six hundred people employed in the Pantin and Aubervilliers works in France, despite the use of "stick" phosphorus in "dipping" mixtures, there was not a single untoward result chronicled during 1896 or 1897 which may be considered phenomenal
For some years the French government has sough newer and more effective and safe methods of match manufacture, and it is constantly, by subsidies, foster ing investigations along these lines. The demand of the hour is for a match that will ignite anywhere by friction, that will be free from phosphorus, and that can be manufactured cheaply. The two first desiderata have been worked out, but thus far are effectually handicapped on the score of economy of production It would seem as if a few hints might be had from Japanese sources. In the "Eastern Insular Empire" great variety of matches are made, some unique ome startling in the results produced, some from pa per, some that ignite without flame, yielding only a coal of fire that persists for several minutes and suita ble for the pipe; but their production is in the hand of guilds, who guard their secrets most jealously and wh as yet have made no organized attempts at expor tation.
The so-called safety match is made with amorphous phosphorus, which also, to insure better ignition though it should not-appears in the prepared surface that aulheres to the container. The "safety" element noreover is soinewhat delusive, smee the sparks that attend the ignition fly to considerable distances and may be-and often are-sources of small fires or even conflagrations. Neither is the prepared surface essential, since these matches may be readily "struck" by passing quickly and lightly over a smooth, dry surace, such as plate glass or polished marble, wood, or metal.

Light is diminished by the interception of glass, as follows: British polished plate, 14 inch thick, 13 per ent; rough cast plate, $1 / 4$ inch thick, 30 per cent rough rolled, $1 / 4$ inch thick, 53 per cent; sheet glass, 32 ounces, 22 per cent.

